

1. Approximate by using the change of base formula. Include at least 3 decimals in your answer.

- a)  $\log_8(63) \approx 1.9924$
- b)  $\log_5(17) \approx 1.7604$
- c)  $\log_{23}(11) \approx 0.7648$
- d)  $\log_{6.6}(66) \approx 2.2202$
- e)  $\log_{0.5}(3) \approx -1.58496$

2. Solve the equation

$$4^{5x+13} = 6^{7-8x}$$

$$\begin{aligned} \ln(4^{5x+13}) &= \ln(6^{7-8x}) \\ (5x+13)\ln(4) &= (7-8x)\ln(6) \\ (5\ln(4))x + 13\ln(4) &= 7\ln(6) - (8\ln(6))x \\ (5\ln(4))x + (8\ln(6))x &= 7\ln(6) - 13\ln(4) \\ (5\ln(4) + 8\ln(6))x &= 7\ln(6) - 13\ln(4) \\ x &= \frac{(7\ln(6) - 13\ln(4))}{(5\ln(4) + 8\ln(6))} \end{aligned}$$

3. Solve the equation

$$(e^x)^2 - 8e^x + \frac{48}{4} = 0$$

quadratic in  $e^x$ :

$$e^x = \frac{8 \pm \sqrt{64 - 4(1)(\frac{48}{4})}}{2} = \frac{8 \pm \sqrt{64 - 48}}{2}$$

$$= \frac{8 \pm \sqrt{16}}{2} = \frac{8 \pm 4}{2} = 4 \pm 2$$

$$\left. \begin{array}{l} \text{So } e^x = 4+2=6 \\ \text{or } e^x = 4-2=2 \end{array} \right\} \text{ so}$$

$$\boxed{\begin{array}{l} x = \ln(6) \\ x = \ln(2) \end{array}}$$

important  
final  
answer.

4. Solve the compound interest formula for  $t$  using only natural logarithms:

$$A = P \left(1 + \frac{r}{n}\right)^{nt}$$

$$\ln(A) = \ln\left(P \left(1 + \frac{r}{n}\right)^{nt}\right)$$

$$\ln(A) = \ln(P) + \ln\left(\left(1 + \frac{r}{n}\right)^{nt}\right)$$

$$\ln(A) = \ln(P) + nt \ln\left(1 + \frac{r}{n}\right)$$

$$\ln(A) - \ln(P) = nt \ln\left(1 + \frac{r}{n}\right)$$

$$\boxed{\frac{\ln(A) - \ln(P)}{n \ln\left(1 + \frac{r}{n}\right)} = t}$$

5. Solve the equation

$$e^x - 40e^{-x} = -6$$

$$\times e^x \quad | \quad \quad \quad | \quad \times e^x$$

$$(e^x)^2 - 40 = -6e^x$$

$$(e^x)^2 + 6e^x - 40 = 0$$

quadratic in  
 $e^x$

$$e^x = \frac{-6 \pm \sqrt{36 - 4(-40)}}{2} = \frac{-6 \pm \sqrt{196}}{2}$$

$$= \frac{-6 \pm 14}{2}$$

$$\text{so } e^x = \frac{-20}{2} = -10$$

$\times$  can't happen!  
(why?)

(so)

$$e^x = \frac{8}{2} = 4$$

$$x = \ln(4)$$